

EDEXCEL FOUNDATION

Stewart House 32 Russell Square London WC1B 5DN

June 2002

Advanced Subsidiary /Advanced Level

General Certificate of Education

Subject **STATISTICS 6688**

Paper No. **S6**



Question number	Scheme	Marks
<p>1a</p> <p>b</p>	<p>(a) parametric - tests the value of a parameter when you know the distribution (or can apply the central limit theorem).</p> <p>non-parametric - tests the value of a parameter when you don't know the distribution</p> <p><i>alter - if say know distribution is normal and is not normal B1 B0</i></p> <p>(b) The Wilcoxon rank sum test is used in <u>two sample problems</u> and the Wilcoxon signed-ranks test is used in <u>one sample problems</u> and in <u>matched pairs problems</u>.</p>	<p>B1</p> <p>B1 (2)</p> <p>B1</p> <p>B1 (need one sample & matched) (2)</p>
<p>2.</p>	<p>$H_0: m_V - m_A = 0$</p> <p>$H_1: m_V - m_A > 0$</p> <p>+++ - + - ++</p> <p><i>X represents the number of + signs</i></p> <p>$X \sim B(8, \frac{1}{2})$</p> <p>$P(X \geq 6) = 1 - P(X \leq 5) = 0.1445 > 0.05$</p> <p>There is not enough evidence to reject H_0. Objects presented visually are not recalled more accurately than objects presented aurally.</p>	<p>B1</p> <p>B1</p> <p><i>used B10 M1</i></p> <p>A1</p> <p><i>x > 6</i></p> <p>M1 A1</p> <p>M1 comp 0.05</p> <p>A1✓</p> <p>(8)</p>

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3.	<p>H_0 : median = 72 H_1 : median \neq 72</p> <p>values -12 -9 3 -2 -8 -22 -5 6 -7 1 rank 9 8 <u>3</u> 2 7 10 4 <u>5</u> 6 <u>1</u></p> <p>$S^+ = 9$</p> <p>$n = 10$. At 0.025 $S = 8$</p> <p>Since 9 is not in the critical region there is not enough evidence to reject H_0 that the median = 72</p>	<p>B1 B1</p> <p>M1 M1</p> <p>A1</p> <p>B1</p> <p>M1 A1√ (8)</p>
4a	<p>(a) $\hat{\beta} = \frac{S_{xy}}{S_{xx}} = \frac{12.5}{6.8} = 1.84$</p> <p>$\hat{\alpha} = 0.483$</p> <p>(b) H_0 : $\beta = 1.5$ H_1 : $\beta \neq 1.5$</p> <p>$RSS = 42.3 - \frac{(12.5)^2}{6.8} = 19.32205\dots$</p> <p>$s^2 = 2.415257\dots$ or $s = 1.5541\dots$</p> <p>$t = \frac{1.838 - 1.5}{1.55/\sqrt{6.8}} = 0.56753\dots$</p> <p>Since $0.5672 < 2.306$, accept H_0 that $\beta = 1.5$</p> <p>After allow (b) H_0 : $\beta = 1.5$ H_1 : $\beta > 1.5$ the $0.5672 < 1.860$ accept H_0 that $\beta = 1.5$</p>	<p>3 s f M1 A1</p> <p>3 s f A1 (3)</p> <p>both B1</p> <p>M1 A1</p> <p>A1</p> <p>0.567 - 0.57 M1 A1</p> <p>comp : 2.306 M1 A1√ (8)</p>

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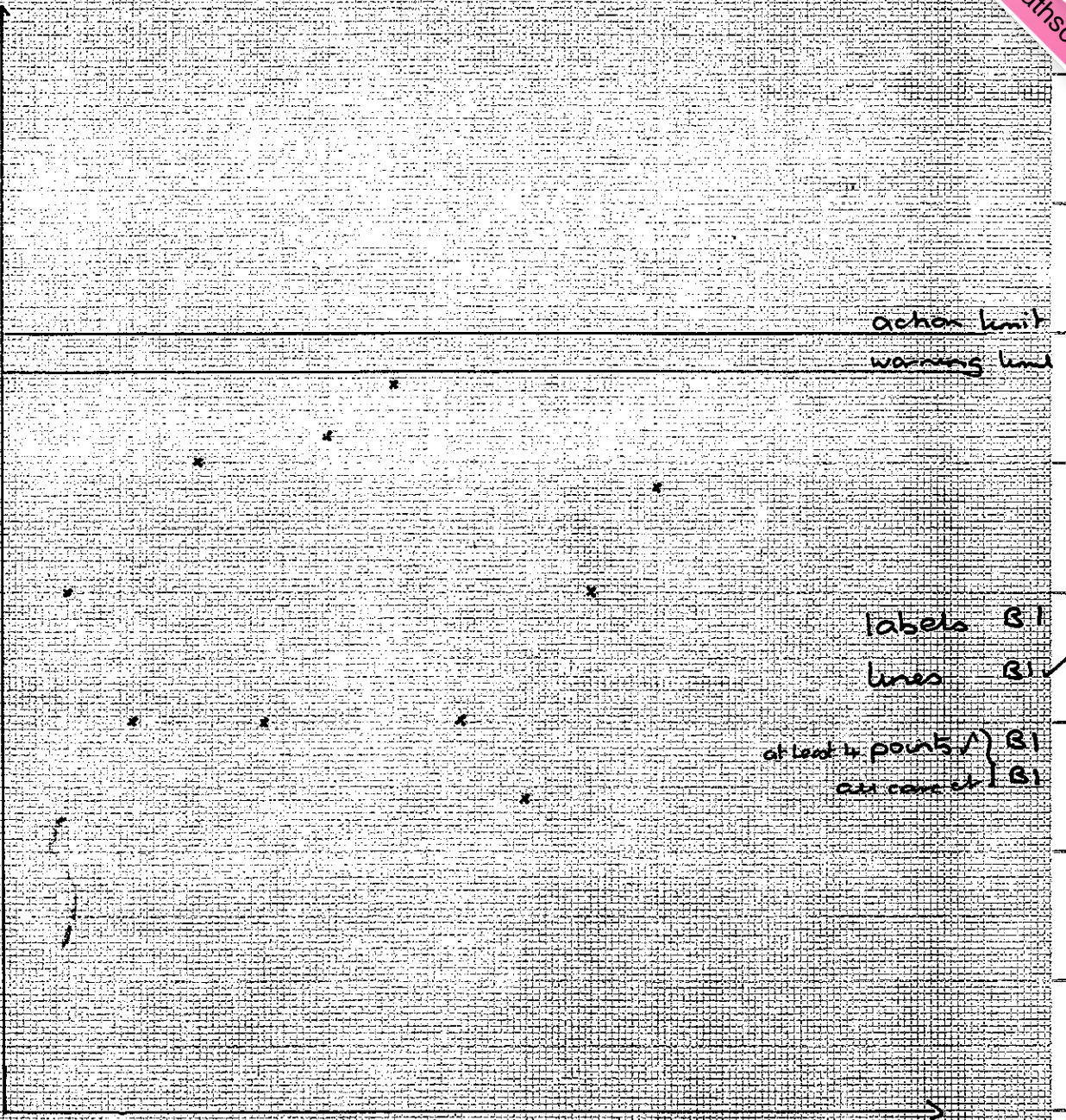
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5. a	$(a) p = \frac{200}{250 \times 10} = 0.08$	M1 A1 (2)
b	$(b) \text{ action limits are } 0.08 + 1.96 \sqrt{\frac{0.08 \times 0.92}{250}}$ <p style="text-align: center;">i.e. 0.114 awrt</p> $\text{warning limits are } 0.08 + 2.3263 \sqrt{\frac{0.08 \times 0.92}{250}}$ <p style="text-align: center;">i.e. 0.120 awrt</p> <p>See graph paper</p>	1.96 M1 B1 A1 2.3263 B1 A1 (2) (7)
c	(c) Points plotted	(2) (2)
d	(d) The process is performing within acceptable limits so far.	B1 (1)

5 etc)

Fraction defective



action limit
warning limit

labels S1
lines S1

at least 4 points ✓ } S1
all correct ✓ } S1

2
2

Sample number

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6a	<p>(a) H_0 : median of girls = median of boys. H_1 : median of girls \neq median of boys.</p> <p>15 17 18 20 22 23 26 27 29 30 38 39 <u>1</u> <u>2</u> <u>3</u> 4 5 <u>6</u> 7 <u>8</u> 9 10 11 12</p> <p>$T = 1 + 2 + 3 + 6 + 8$ $= 20$</p> <p>Two tail test therefore use $2\frac{1}{2}\%$</p> <p>critical value is 20</p> <p>20 is in the critical region and therefore we reject H_0 in favour of H_1. There is evidence that there is a difference between the time girls and boys take to solve the puzzle.</p>	<p>both B1</p> <p>all together M1 M1 } cler</p> <p>M1 A1</p> <p>B1</p> <p>A1 ✓ (7)</p>
b	<p>(b) H_0 : median of girls = median of boys. H_1 : median of girls $>$ median of boys.</p> <p>$n_1 = 25$ $n_2 = 25$</p> <p>$N (637.5, 2656.25)$</p> <p>$T = 798$</p> <p>$\frac{797.5 - 637.5}{\sqrt{2656.25}} = 3.104$</p> <p>one tail test 5% significance level critical value = 1.6449</p> <p>3.104 $>$ 1.645 there is evidence that boys are quicker at solving the puzzle than girls.</p>	<p>both B1</p> <p>M1 A1 A1</p> <p>M1 A1 $\pm \frac{1}{2}$</p> <p>B1</p> <p>A1 ✓ (8)</p>

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7a	(a) Allocate bunches of flowers <u>at random</u> , 4 to each liquid.	B1 B1 (2)																																																							
b	(b) Randomised block design.	B1 (1)																																																							
c	(c) <table border="1" style="margin: 10px auto;"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>W</td> <td>12</td> <td>13</td> <td>9</td> <td>10</td> <td>44</td> </tr> <tr> <td>L & W</td> <td>14</td> <td>15</td> <td>10</td> <td>9</td> <td>48</td> </tr> <tr> <td>W + C</td> <td>13</td> <td>16</td> <td>11</td> <td>10</td> <td>50</td> </tr> <tr> <td>Total</td> <td>39</td> <td>44</td> <td>30</td> <td>29</td> <td>142</td> </tr> </tbody> </table> <p>Correction Factor = $\frac{(142)^2}{12} = 1680.33$</p> <p>Total SS = $1742 - 1680.33 = 61.67$</p> <p>Type SS = $\frac{1}{3} \{39^2 + 44^2 + 30^2 + 29^2\} - 1680.33 = 52.33$</p> <p>Liquid SS = $\frac{1}{4} \{44^2 + 48^2 + 50^2\} - 1680.33 = 4.66$</p> <table border="1" style="margin: 10px auto;"> <thead> <tr> <th>Source</th> <th>df</th> <th>SS</th> <th>MSS</th> <th>Ratio</th> </tr> </thead> <tbody> <tr> <td>Between Types</td> <td>3</td> <td>52.33</td> <td>17.44</td> <td>22.43</td> </tr> <tr> <td>Between Liquids</td> <td>2</td> <td>4.67</td> <td>2.33</td> <td>3.00</td> </tr> <tr> <td>Residual</td> <td>6</td> <td>4.66</td> <td>0.778</td> <td></td> </tr> <tr> <td>Total</td> <td>11</td> <td>61.67</td> <td></td> <td></td> </tr> </tbody> </table>		A	B	C	D	Total	W	12	13	9	10	44	L & W	14	15	10	9	48	W + C	13	16	11	10	50	Total	39	44	30	29	142	Source	df	SS	MSS	Ratio	Between Types	3	52.33	17.44	22.43	Between Liquids	2	4.67	2.33	3.00	Residual	6	4.66	0.778		Total	11	61.67			M1 M1 M1 3, 2, 6 B1 Residual M1 Ratio M1 A1 A1
	A	B	C	D	Total																																																				
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7 cont	<p>$\mu_w = \mu_c = \mu_e$</p> <p>H_0: Liquids do not affect length of time flowers live. H_1: Liquids do affect length of time flowers live. <i>not all means are equal</i></p> <p>$F_6^2 > 10.9$</p> <p>3 is not in critical region therefore not enough evidence to reject H_0, <i>the liquid has no affect on the length of time flowers live.</i></p> <p>(d) H_0: Different types of flowers do not live different lengths of times. <i>or $\mu_A = \mu_B = \mu_C = \mu_D$</i> H_1: Different types of flowers do live different lengths of times. <i>or not all means are equal</i></p> <p><u>$F_6^3 > 9.78$</u></p> <p>$22\frac{3}{4} = 22.75$ is in the critical region so there is evidence to reject H_0. Different types of flowers do live different lengths of time.</p>	<p>B1</p> <p>B1</p> <p>A1 ✓ (11)</p> <p>B1</p> <p>M1</p> <p>A1 ✓ (3)</p>